## Intermediate Check In - 6.01 Algebraic expressions

1. Express the following as a simplified single expression.

$$
(2 x+3)-(x-2)
$$

2. Simplify the following algebraic expression.

$$
x^{2} \times 2 x^{5} \times x
$$

3. Multiply out and simplify the following expression.

$$
(x+2)(3 x-1)
$$

4. Factorise the following expression.

$$
x^{2}-7 x+10
$$

5. Express the following as a simplified single expression.

$$
4 x^{4} y^{2} \div 2 x^{3} y^{2}
$$

6. Explain why $x^{2}-6 x+9 \equiv(x-3)^{2}$ is an identity but $x^{2}-5 x+10=(x-3)^{2}$ is an equation.
7. The area of a rectangle is given as $x^{2}+5 x+4$. Show that the perimeter of the rectangle is $2(2 x+5)$.
8. Show that $a \%$ of $b$ is the same as $b \%$ of $a$.
9. The diagram on the right shows a square with sides of length $2 x$. Write down an expression for the area of the triangle marked on one corner.

10. The area of a chessboard is given as $64 x^{2}-256 x+256 \mathrm{~cm}^{2}$. Find an expression for the length of a single square on the board.

## Extension

$1,1,2,3,5 \ldots$ and $2,5,7,12,19 \ldots$ are examples of Fibonacci sequences. Show that the sum of the first ten terms of any Fibonacci sequence is always $11(5 a+8 b)$ where $a$ and $b$ are the first 2 terms.

## Answers

1. $x+5$
2. $2 x^{8}$
3. $3 x^{2}+5 x-2$
4. $(x-2)(x-5)$
5. $2 x$
6. $x^{2}-6 x+9 \equiv(x-3)^{2}$ is an identity because it is true for all values of $x$, but $x^{2}-5 x+10=(x-3)^{2}$ is an equation because it is only true when $x=-1$.
7. $x^{2}+5 x+4=(x+4)(x+1)$ so the length is $x+4$ and the width is $x+1$, giving a perimeter of $4 \mathrm{x}+10=2(2 x+5)$.
8. $\frac{a}{100} \times b=\frac{a b}{100}=\frac{b}{100} \times a$
9. Area $=\frac{1}{2}(2 x-2)(2 x-2)=2 x^{2}-4 x+2$
10. Factorising by the number of squares gives $64\left(x^{2}-4 x+4\right)$, then factorising again to find the length of the side of each square gives $x^{2}-4 x+4=(x-2)(x-2)$. Side length is $x-2 \mathrm{~cm}$.

## Extension

$a, b, a+b, a+2 b, 2 a+3 b, 3 a+5 b, 5 a+8 b, 8 a+13 b, 13 a+21 b, 21 a+34 b$.
Sum of the first ten terms is $55 a+88 b=11(5 a+8 b)$.

[^0][^1]| Assessment <br> Objective | Qu. | Topic | R | A | G |
| :---: | :---: | :--- | :---: | :---: | :---: |
| AO1 | 1 | Simplify an algebraic expression by collecting like terms |  |  |  |
| AO1 | 2 | Simplify algebraic products using the laws of indices |  |  |  |
| AO1 | 3 | Expand and simplify a binomial product |  |  |  |
| AO1 | 4 | Factorise a quadratic expression into brackets |  |  |  |
| AO1 | 5 | Simplify algebraic quotients using the laws of indices |  |  |  |
| AO2 | 6 | Understand the difference between an equation and an <br> identity |  |  |  |
| AO2 | 7 | Factorise and collect like terms to derive a length from an <br> area |  |  |  |
| AO2 | 8 | Use algebra to generalise a mathematical concept |  |  |  |
| AO3 | 9 | Use algebra to solve a geometric problem |  |  |  |
| AO3 | 10 | Use algebra to solve a contextual geometric problem |  |  |  |


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[^1]:    OCR Resources: the small print
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